

# COMPARATIVE PERFORMANCE ANALYSIS OF FCFS, JOHNSON SEQUENCING AND DYNAMIC MAX-MIN JOHNSON SEQUENCING (DMMJS) ALGORITHM USING THREE SERVERS IN CLOUD COMPUTING ENVIRONMENT

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*This paper presents Dynamic Max-Min Johnson scheduling algorithm that offers the optimal sequence. Johnson's rule is perhaps the most classical algorithm in the scheduling field. Dynamic Max-Min Johnson scheduling algorithm gives the most excellent way to the system flow shop to reduce the makespan in polynomial time. The sequencing problem offers with determining a most useful series of acting a number of tasks via a finite number of machines in line with some pre-assigned order with a view to optimize the output. The goal is to decide on the most desirable order of performing the jobs in such a manner that the full elapsed time may be minimal.*

**Keywords:** Cloud computing, Job scheduling, FCFS, Johnson scheduling, Dynamic Max-Min Johnson Sequencing algorithm.

## 1. Introduction

In today's world Cloud computing is very widely used architecture. In simple words, Cloud computing means permitting dynamic allocation of resources, strolling applications using data centers and networks to remote customers [1]. By using Cloud computing, it will help customers in many ways like, ability at runtime without buying new infrastructure, it will also help different business, cooperation and industry in storing their data properly. Currently many company [2] are providing cloud computing services like Google, Microsoft etc. Johnson sequencing rule basically helps in scheduling of different jobs. The primary motive of Johnson rule is to decrease the total idle time of machines & decrease the total time taken to finish all the different jobs. As there aren't any priority rules due to the fact all activity has equal priority, sequencing the jobs in line with the time taken may additionally decrease the total idle time taken by the different jobs [3]. DMMJS algorithm is widely adopted in complex engineering task and Scheduling problem to optimize Cost efficiency and productivity. In this paper, we are providing an algorithm which can adequately increase the availability of resource when demand of resource increases in parallel

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processing of cloud environment. The second major contribution is to reduce the overhead of resource management in equally distributed data center to multiple tenant user infrastructures.

This research paper is organized as follows. Section 1 describes Introduction, Section-2 highlight major literature gap, Section-3 proposes major algorithm formulation of proposed Literary Review, Section -4 scatters the results with future scope and conclusion.

<b>Nomenclatures</b>	
$\lambda$	Average arrival rate of task
$\tau$	Time between two successive arrivals of task
$S_i$	Service time of $i^{\text{th}}$ task
$\mu$	Service rate
$P_0$	Probability that system is idle
$L_q$	In a queue mean number of tasks waiting
$L_s$	In a system mean number of tasks waiting
$W_q$	In a queue mean waiting time of tasks
$W_s$	In a system mean waiting time of tasks
<b>Abbreviations</b>	
<i>CSP</i>	Cloud Service Provider
<i>SC</i>	Service Centre
<i>FCFS</i>	First Come First Serve
<i>RR</i>	Round Robin
<i>JS</i>	Johnson Sequencing
<i>DMMJS</i>	Dynamic Max-Min Johnson Sequencing
<i>DCC</i>	Data Centre Controller

## 2. Literature review of the related work

The main research problem is the jobs allocation in cloud in the arena of cloud computing environment. The main issue is to minimize the waiting time while applying Task allocations algorithms and to gain maximum profit. The principal design is to decrease the execution time of the undertaking by utilizing a different task allocation algorithm [4]. There are various sorts of task allocation algorithm present in cloud climate which can't be applied to cloud environments, since cloud is a circled environment that contains heterogeneous structures. Some fundamental algorithms that are used in task allocations are FCFS algorithm in which the task which comes first will execute first. However, the main problem is the amount of time tasks spend waiting in the queue. A new algorithm, called Johnson Sequencing, was then proposed [5]. It fixed the problem with FCFS, which was the average amount of time tasks spent waiting, and it was followed by

the Dynamic Max-Min Johnson Sequencing algorithm, which will further reduce task waiting times.

### 3. System design of Johnson Sequencing

This part deals with scheduling and queuing model as shown in fig.1. In scheduling phase Johnson Algorithm is applied to schedule at Task and M/M/c/K queuing is executed to find holding time. Here  $n$  number of task in the system. JS Calculation has been viewed as giving an ideal succession of occupations [6]. Models for lining frameworks like M/M/c/K are considered into a record to ascertain AWT. There is a large number of clients who submit requests to the cloud broker, and the requested resource may be infrastructure-, resource-, platform-, storage-, or software-based [7]. Cloud broker detects and has management skills as an intermediary service. The monitor records all user requests, jobs, and resource information for a predetermined amount of time [8]. Analyzer then determines the resources that are available. The required resources are provided in accordance with the SLA service terms and conditions, depending on their availability [9]. When the scheduler module receives information about the available resources, it schedules the tasks using the Johnson Algorithm, which determines the best order and minimizes the make span, hence reducing client wait times. The M/M/c/K system allows for the passing of scheduled jobs, which results in a variety of waiting periods that will be covered later. The sharing of the system may be maximized by efficient server use. By using the servers effectively, the system's sharing potential may be maximized [10].

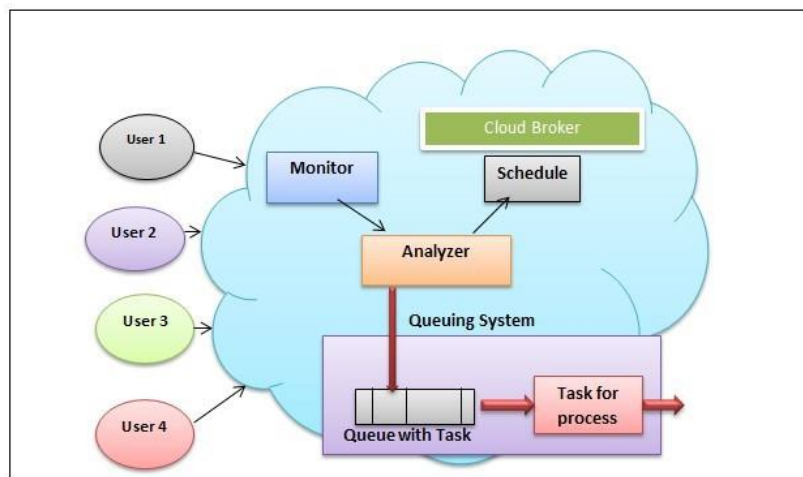


Fig. 1. System design of M/M/c/K Queuing system.

#### 4. Flow chart of FCFS Algorithm

As seen in Fig. 2, FCFS operates under the tenet of "First Come, First Serve." The first task which comes first will be executed first. A non-primitive scheduling technique is used here [11]. In this diagram, the client requests are handled by the DCC, who then places them all in a FIFO queue and routes them to the FCFS virtual machines. The client request is carried out if there are available virtual machines.

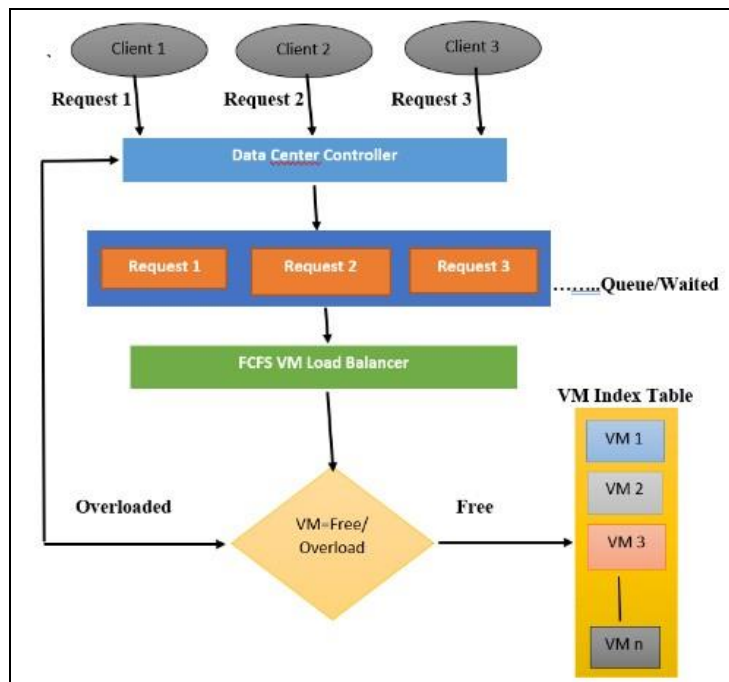


Fig.2.Flow Chart of FCFS Algorithm

#### 5. Lining model for distributed computing climate

The study of the wonder of the holding line is known as queuing theory. By demonstrating entrance preparation, the service process, the number of servers, and the locations with the highest capacity, the fundamental queuing process is completely illustrated [12]. Recognizing that each work's method time should be seen as an exponential transmission It is possible to build an M/M/c/K lined demonstration with non-preemptive demonstration using two servers, S1 and S2, and five locations of holding up positions as capacity [13]. In this study, the queuing model and work scheduling are combined. The fact that page hits start at time zero has been taken into account. We require a rough estimate of "" in order to demonstrate this distribution. Considering that the interval between two subsequent arrivals is "", Therefore, we presume that "" = interval-arrival time.

So average arrival rate

$$\lambda = \frac{1}{E[\tau]} \text{ where } E[\tau] = \text{Average inter-Arrival Time.} \quad (1)$$

$$\text{Average Service time } E(S) = \frac{\sum_{i=0}^n S_i}{n} \quad (2)$$

$$\text{and Service rate will be } \mu = \frac{1}{E(S)} \quad (3)$$

Probability that the system is idle

$$P_0 = \left[ \sum_{n=0}^{S-1} \frac{1}{n!} \left( \frac{\lambda}{\mu} \right)^n + \frac{1}{S!} \left( \frac{\lambda}{\mu} \right)^S \left( \frac{S\mu}{S\mu - \lambda} \right) \right]^{-1} \quad (4)$$

Average number of tasks waiting in the queue

$$L_q = \left[ \frac{1}{(S-1)!} * \left( \frac{\lambda}{\mu} \right)^S * \left( \frac{\lambda\mu}{(S\mu - \lambda)^2} \right) \right] * P_0 \quad (5)$$

Average number of tasks in the system

$$L_s = L_q + \frac{\lambda}{\mu} \quad (6)$$

Average waiting time of tasks in queue

$$W_q = \frac{L_q}{\lambda} \quad (7)$$

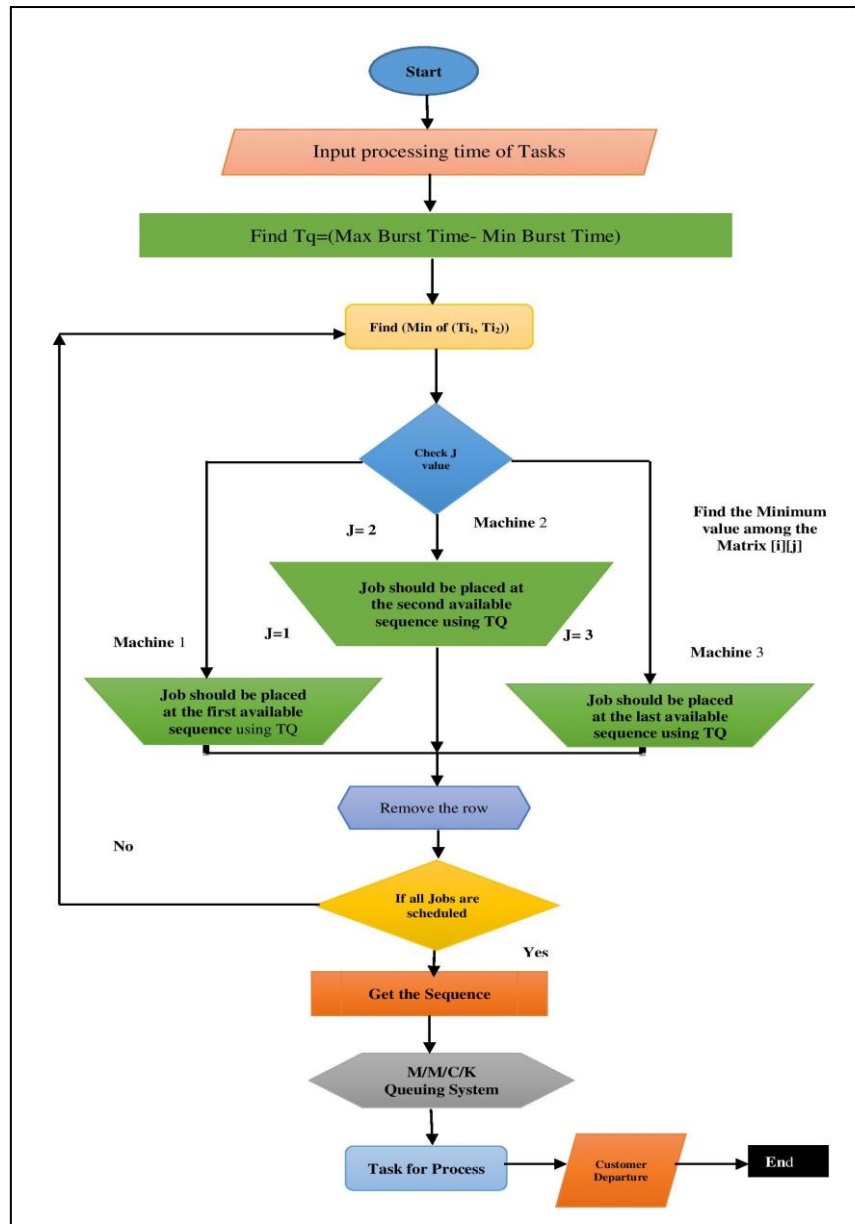
Average waiting time of tasks in the system

$$W_s = W_q + \frac{1}{\mu} \quad (8)$$

## 6. Objective of the study

Here, a system has been created where Dynamic Max-Min Johnson Sequencing has been used using three servers in the cloud to decrease the service time in the cloud. Let's suppose a batch has a variety of jobs. Creating a Gantt chart will help in calculating the service time. The total execution time of each task is shown in the Gantt chart. After the use of the Dynamic Max-Min Johnson Sequencing Rule in the system, the common range of clients within the queue and inside the machine could be decreased, in addition to the average waiting time inside the device and in the queue.

## 7. Dynamic Max-Min Johnson Sequencing Algorithm Flowchart



## 8. System flow

In the system design, there are total 4 jobs and every job have a processing time which are available in a table shown below. A, B, C are the Machines and P1,P2,P3,P4 are the number of jobs.

Table 1

Processing time Matrix of Three Machines			
Task or Jobs	Machine A(MC <sub>A</sub> )	Machine B(MC <sub>B</sub> )	Machine C(MC <sub>C</sub> )
P1	AA <sub>1</sub>	BB <sub>1</sub>	CC <sub>1</sub>
P2	AA <sub>2</sub>	BB <sub>2</sub>	CC <sub>2</sub>
P3	AA <sub>3</sub>	BB <sub>3</sub>	CC <sub>3</sub>
P4	AA <sub>4</sub>	BB <sub>4</sub>	CC <sub>4</sub>

### 8.1 Converting 3 machines to 2 machines

**Step 1:** Find the Minimum of (AA<sub>i</sub>) , Maximum of (BB<sub>i</sub>) and Minimum of(CC<sub>i</sub>)

**Step 2:** Now verify the following condition. Minimum of (AA<sub>i</sub>) >= Maximum of (BB<sub>i</sub>) and Minimum of (CC<sub>i</sub>) >= Maximum of(BB<sub>i</sub>).If at least one condition is satisfied then we can convert 3 machines into 2 machines. If none of the condition are satisfied then the method cannot be applied.

**Step 3:** If any of the above condition is satisfied then, Converting MA, MB and MC into new machine GG and HH. For calculating Machine G add the processing time of (MCA) and (MCB) for each job. That is Machine [14].

$$GG = AA_i + BB_i$$

For calculating Machine H add the processing time of (MCB) and (MCC) for each job. That is Machine HH = CC<sub>i</sub> + BB<sub>i</sub>

**Step 4:** Now apply Johnson's sequencing Algorithm for n-jobs and 2-machines to determine the optimal sequence. Conversion of 3 Machine to 2 Machine is shown in table 2.

Table 2

Executing time Matrix		
Job	(MC <sub>A</sub> )	(MC <sub>B</sub> )
P1	GG <sub>1</sub>	HH <sub>1</sub>
P2	GG <sub>2</sub>	HH <sub>2</sub>
P3	GG <sub>3</sub>	HH <sub>3</sub>
P4	GG <sub>4</sub>	HH <sub>4</sub>

### 8.2 Johnson's sequencing Algorithm for 2 machines.

Step 1: Check the GG<sub>i</sub>'s and HH<sub>i</sub>'s for i = 1, 2,.....n and then calculate the minimum of [GG<sub>i</sub> , HH<sub>i</sub>]

Step 2: If the minimum be GG<sub>k</sub> for some i = k, do the kth job first of all. And, if this minimum be HH<sub>k</sub> for some i = r, do the rth job last of all [15].

Step 3: If there is a equal value for the minimum  $GG_k = HH_k$ , process the  $k$ th job first of all and the  $r$ th job last of all. If there is an equal value for the minimum occurs among the  $GG_i$ 's select the job corresponding to the minimum of  $HH_i$ 's and process it first of all. If the equal for min occurs among the  $HH_i$ 's take the job corresponding to the min of  $GG_i$ 's and process it last of all [16].

Step 4: Then, mark the jobs which is already done and then repeat from steps one to step three arranging the jobs next to first or next to last, until all the tasks will be completed [17].

Table 3

Initial Processing Time of different task				
Tasks	Processing Time of Server Machine1 (in Millisecond)	Processing Time of Server Machine2 (in Millisecond)	Processing Time of Server Machine3 (in Millisecond)	Burst Time
P1	0.04	0.02	0.09	0.15
P2	0.03	0.02	0.09	0.14
P3	0.09	0.05	0.10	0.24
P4	0.02	0.01	0.06	0.09

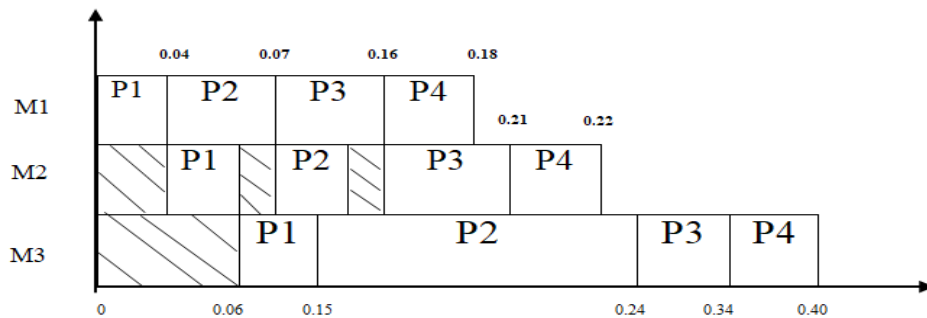


Fig.4. Gantt Chart of FCFS Algorithm

Now, calculating the service time of every process with the help of above Gantt chart.

$$\text{Job P1: } 0.15 - 0 = 0.15$$

$$\text{Job P2: } 0.24 - 0.04 = 0.20$$

$$\text{Job P3: } 0.34 - 0.07 = 0.27$$

$$\text{Job P4: } 0.40 - 0.16 = 0.24$$

$$\text{Mean service time} = E(s) = 0.86/4 = 0.215$$

$$\text{Now, calculating the service rate } \mu = 1/(E(s)) = 1/0.215 = 4.6511$$

$$P_o (\text{for FCFS}) = 0.30264$$



Table 4

**In-Out time of Three Machines of different tasks in Johnson Sequencing Algorithm**

Tasks	Machine1		Machine2		Machine3	
	IN TIME	OUT TIME	IN TIME	OUT TIME	IN TIME	OUT TIME
<b>P4</b>	0	0.02	0.02	0.03	0.03	0.09
<b>P2</b>	0.02	0.05	0.05	0.07	0.09	0.18
<b>P1</b>	0.05	0.09	0.09	0.11	0.18	0.27
<b>P3</b>	0.09	0.18	0.18	0.23	0.27	0.37

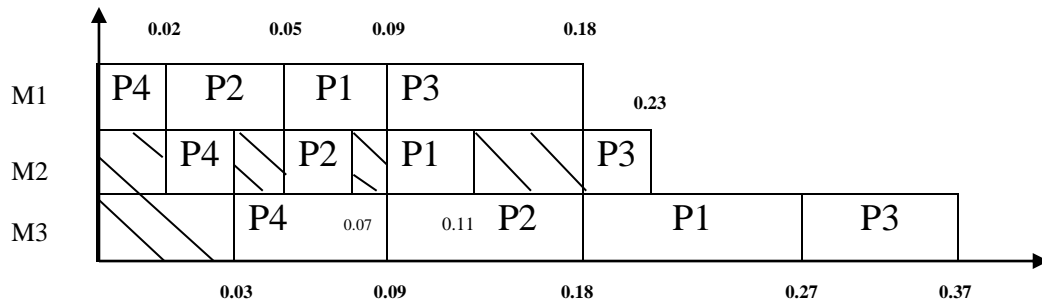


Fig.5. Gantt Chart of Johnson Sequencing Algorithm

Now, calculating the service time of every process with the help of above Gantt chart.

$$\text{Job P4: } 0.09 - 0 = 0.09$$

$$\text{Job P2: } 0.18 - 0.02 = 0.16$$

$$\text{Job P1: } 0.27 - 0.05 = 0.22$$

$$\text{Job P3: } 0.37 - 0.09 = 0.28$$

$$\text{Mean service time} = E(s) = 0.75/4 = 0.1875$$

$$\text{Now, calculating the service rate } \mu = 1/(E(s)) = 1/0.1875 = 5.3333$$

$$P_o \text{ (for JS)} = 0.470592$$

For Dynamic Johnsons sequencing, Time quantum will be calculated first.

Now, calculating the Time quantum

$$TQ = \text{MAX}(BT) - \text{MIN}(BT)$$

$$TQ = 0.24 - 0.09 = 0.15$$

Now, using the time quantum to create Gantt chart

Table 5

**In-Out time of Three Machines of different tasks of Dynamic MaxMin Johnson Sequencing Algorithm**

Tasks	Machine1		Machine2		Machine3	
	IN TIME	OUT TIME	IN TIME	OUT TIME	IN TIME	OUT TIME
<b>P4</b>	0	0.09	0.09	0.62	Idle	Idle
<b>P2</b>	0.09	0.23	Idle	Idle	Idle	Idle
<b>P1</b>	0.23	0.38	Idle	Idle	Idle	Idle
<b>P3</b>	0.38	0.53	Idle	Idle	Idle	Idle

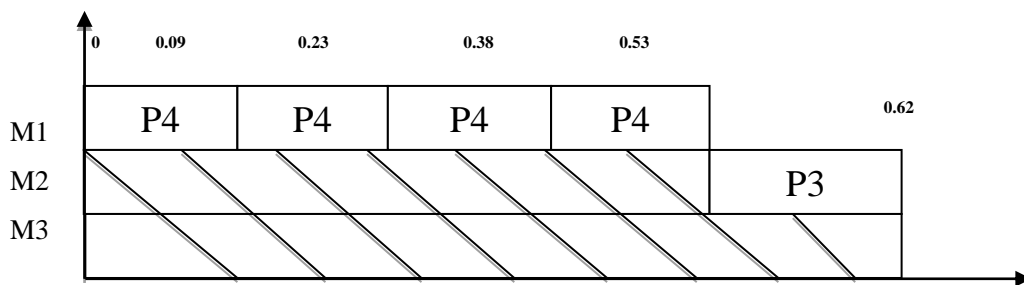


Fig.6. Gantt chart of dynamic max-min Johnson sequencing algorithm

Now, calculating the service time of every process with the help of above Gantt chart.

$$\text{Job P4: } 0.09 - 0 = 0.09$$

$$\text{Job P2: } 0.23 - 0.09 = 0.14$$

$$\text{Job P1: } 0.38 - 0.23 = 0.15$$

$$\text{Job P3: } 0.62 - 0.38 = 0.24$$

$$\text{Mean service time} = E(s) = 0.62/4 = 0.155$$

$$\text{Now, calculating the service rate } \mu = 1/(E(s)) = 1/0.155 = 6.451612$$

$$P_o \text{ (for DMMJS)} = 0.53698$$

## 9. Results

Tables 6, 7, and 8 have each been connected with the findings from the associated formulae. Here, the DMMJS Algorithm reduces service time and average waiting time when compared to the FCFS and Johnson Sequencing. Taking into account the results from formulae (1), (2), (3), (4), (5), (6) (7) and (8). The connection is between  $L_q$ ,  $L_s$ ,  $W_q$ , and  $W_s$ . Fig.7 through 10 show the average number of jobs and average length of the line. A Dynamic Max-Min Johnson sequencing algorithm can reduce it in the system instead of FCFS and the

Johnson sequencing technique. First, we compute the average arrival rate ( $\lambda$ ), and then we figure out the average service time ( $E$ ), which makes the service rate equal to  $\mu = \frac{1}{E(S)}$ . The probability that the system is idle ( $P_0$ ) will then be determined using the formula (4). Using the value of ( $P_0$ ) from the formula (5), the average number of tasks waiting in the queue ( $L_q$ ) is then determined. Following that, the system's average number of tasks ( $L_s$ ) is determined using the preceding  $L_q$  findings from the formula (6). Following that, the formula (7) is used to compute the average waiting time for tasks in the queue, and finally, from the formula (9) is used to determine the average waiting time for tasks in the system (8).

Table 6

Results by using FCFS

	(Lq) in milliseconds	(Ls)in milliseconds	(Wq) in milliseconds	(Ws) in milliseconds
$\lambda=2$	.00078307	.43078307	.000391535	.2153915
$\lambda=3$	.009428535	.654434035	.0024550175	.21745575
$\lambda=4$	.018074	.878085	.0045185	.21952

Table 7

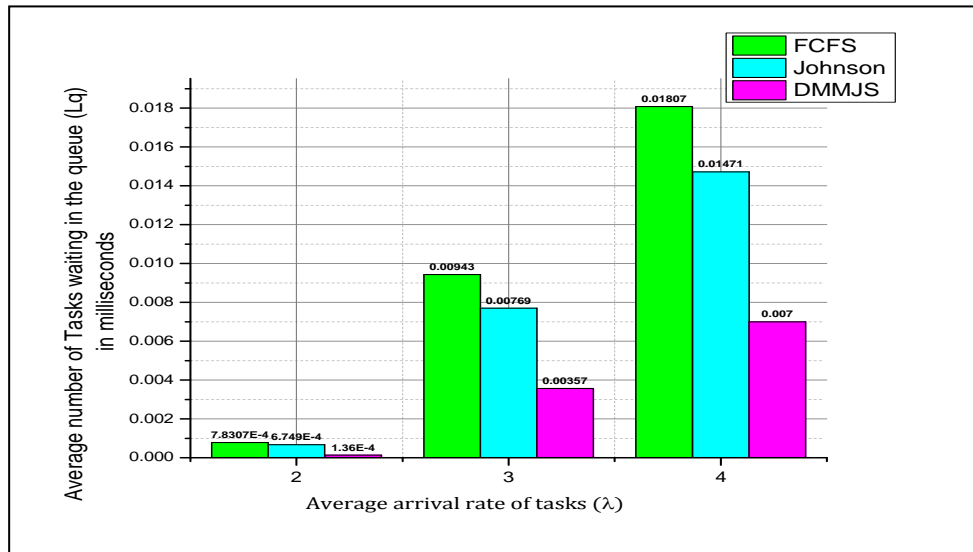
Results by using Johnson Sequencing

	(Lq) in milliseconds	(Ls)in milliseconds	(Wq) in milliseconds	(Ws) in milliseconds
$\lambda=2$	.0006749	.3756749	.00033745	.187849
$\lambda=3$	.00769375	.57019375	.0020078	.189519425
$\lambda=4$	.0147126	.7647126	.00367815	.19118985

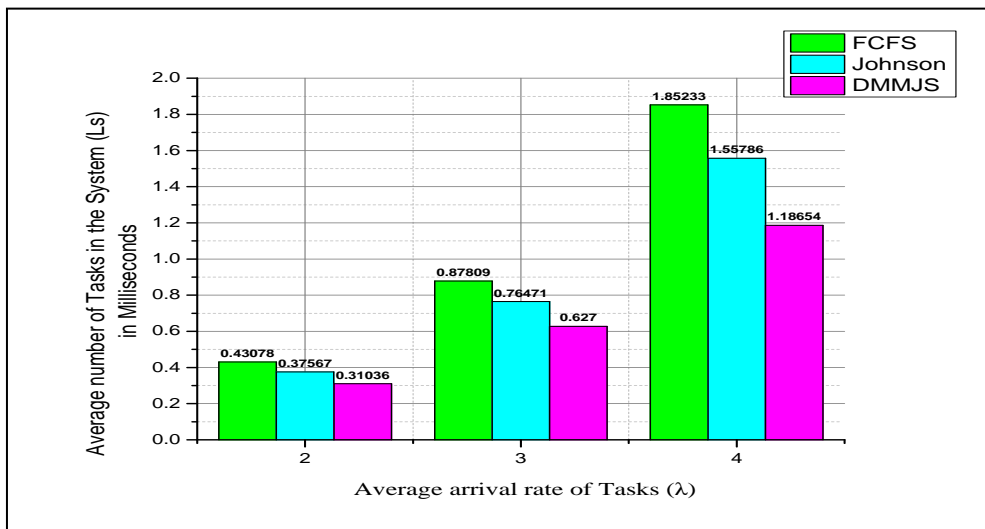
Table 8

Results by using Dynamic Max-Min Johnson Sequencing(DMMJS)

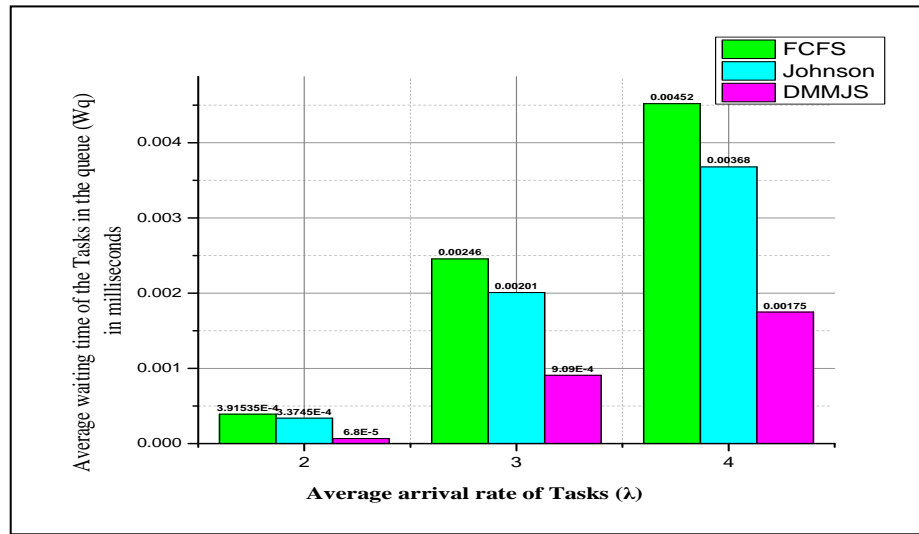
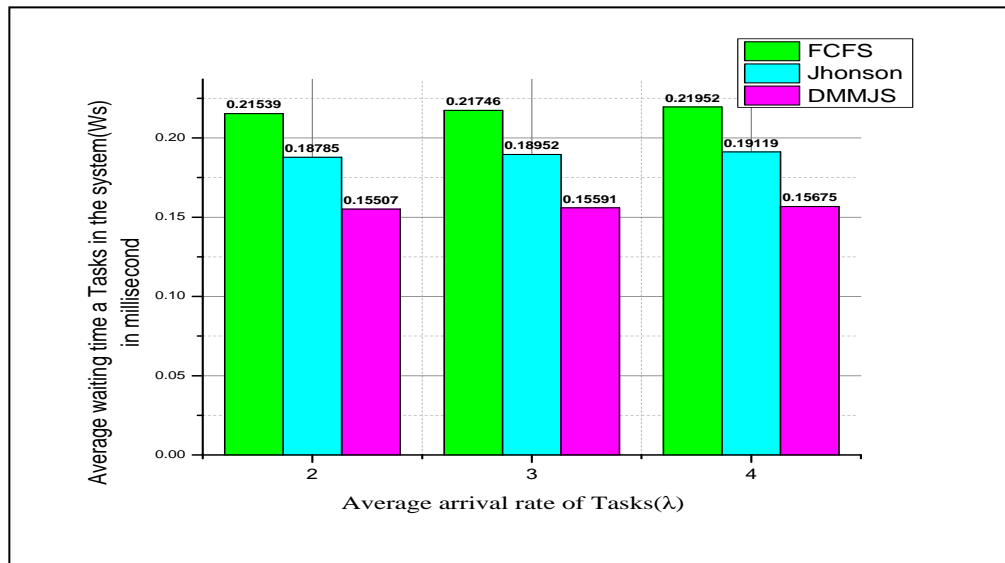
	(Lq) in milliseconds	(Ls)in milliseconds	(Wq) in milliseconds	(Ws) in milliseconds
$\lambda=2$	.000136	.310360	.000068	.155068
$\lambda=3$	.003568	.46868	.000909	.155909
$\lambda=4$	.007	.627	.00175	.15675

Fig.7.  $L_q$  versus Arrival rate of tasks

In this fig.7 the results of the average number of tasks waiting in the queue is shown. Here we can see that a smaller number of tasks are waiting in Dynamic Max-Min Johnson sequencing as compared to Johnson Sequencing and FCFS task scheduling.

Fig.8.  $L_s$  versus Arrival rate of tasks

In Fig.8 and Fig.9, the results of average number of tasks in the queue and system is shown. Here we can see that a smaller number of tasks are waiting in Dynamic Max-Min Johnson sequencing as compared to Johnson Sequencing and FCFS task scheduling.

Fig. 9.  $W_q$  versus Arrival rate of tasksFig.10.  $W_s$  versus Arrival rate of tasks

In this Fig.10 the results of average waiting time of tasks in the system is shown. Here we can see that a smaller number of tasks are waiting in Dynamic Max-Min Johnson sequencing as compared to Johnson Sequencing and FCFS task scheduling.

## 10. Conclusions

Cloud computing is a term that is used often in research and academia nowadays. Utilizing virtualized computer resources, cloud providers distribute

them in accordance with user needs. In this work, we've covered queuing models with many servers and finite capacities as well as scheduling techniques. The Dynamic Max-Min Johnson algorithm was easily created in a suitable setting. Here, we've demonstrated how to obtain a highly valuable sequence using the Dynamic Johnson Sequencing set of rules.

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